

Radicals - Add/Subtract Radicals

Adding and subtracting radicals is very similar to adding and subtracting with variables. Consider the following example.

Example 1.

$$\begin{array}{ll} 5x + 3x - 2x & \text{Combine like terms} \\ 6x & \text{Our Solution} \end{array}$$

$$\begin{array}{ll} 5\sqrt{11} + 3\sqrt{11} - 2\sqrt{11} & \text{Combine like terms} \\ 6\sqrt{11} & \text{Our Solution} \end{array}$$

Notice that when we combined the terms with $\sqrt{11}$ it was just like combining terms with x . When adding and subtracting with radicals we can combine like radicals just like like terms. We add and subtract the coefficients in front of the

radical, and the radical stays the same. This is shown in the following example.

Example 2.

$$\begin{array}{ll} 7\sqrt[5]{6} + 4\sqrt[5]{3} - 9\sqrt[5]{3} + \sqrt[5]{6} & \text{Combine like radicals } 7\sqrt[5]{6} + \sqrt[5]{6} \text{ and } 4\sqrt[5]{3} - 9\sqrt[5]{3} \\ 8\sqrt[5]{6} - 5\sqrt[5]{3} & \text{Our Solution} \end{array}$$

We cannot simplify this expression any more as the radicals do not match. Often problems we solve have no like radicals, however, if we simplify the radicals first we may find we do in fact have like radicals.

Example 3.

$$\begin{array}{ll} 5\sqrt{45} + 6\sqrt{18} - 2\sqrt{98} + \sqrt{20} & \text{Simplify radicals, find perfect square factors} \\ 5\sqrt{9 \cdot 5} + 6\sqrt{9 \cdot 2} - 2\sqrt{49 \cdot 2} + \sqrt{4 \cdot 5} & \text{Take roots where possible} \\ 5 \cdot 3\sqrt{5} + 6 \cdot 3\sqrt{2} - 2 \cdot 7\sqrt{2} + 2\sqrt{5} & \text{Multiply coefficients} \\ 15\sqrt{5} + 18\sqrt{2} - 14\sqrt{2} + 2\sqrt{5} & \text{Combine like terms} \\ 17\sqrt{5} + 4\sqrt{2} & \text{Our Solution} \end{array}$$

This exact process can be used to add and subtract radicals with higher indicies

Example 4.

$$\begin{array}{ll} 4\sqrt[3]{54} - 9\sqrt[3]{16} + 5\sqrt[3]{9} & \text{Simplify each radical, finding perfect cube factors} \\ 4\sqrt[3]{27 \cdot 2} - 9\sqrt[3]{8 \cdot 2} + 5\sqrt[3]{9} & \text{Take roots where possible} \\ 4 \cdot 3\sqrt[3]{2} - 9 \cdot 2\sqrt[3]{2} + 5\sqrt[3]{9} & \text{Multiply coefficients} \\ 12\sqrt[3]{2} - 18\sqrt[3]{2} + 5\sqrt[3]{9} & \text{Combien like terms } 12\sqrt[3]{2} - 18\sqrt[3]{2} \\ - 6\sqrt[3]{2} + 5\sqrt[3]{9} & \text{Our Solution} \end{array}$$

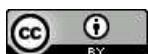


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Practice - Add and Subtract Radicals

Simiplify

- 1) $2\sqrt{5} + 2\sqrt{5} + 2\sqrt{5}$
- 2) $-3\sqrt{6} - 3\sqrt{3} - 2\sqrt{3}$
- 3) $-3\sqrt{2} + 3\sqrt{5} + 3\sqrt{5}$
- 4) $-2\sqrt{6} - \sqrt{3} - 3\sqrt{6}$
- 5) $-2\sqrt{6} - 2\sqrt{6} - \sqrt{6}$
- 6) $-3\sqrt{3} + 2\sqrt{3} - 2\sqrt{3}$
- 7) $3\sqrt{6} + 3\sqrt{5} + 2\sqrt{5}$
- 8) $-\sqrt{5} + 2\sqrt{3} - 2\sqrt{3}$
- 9) $2\sqrt{2} - 3\sqrt{18} - \sqrt{2}$
- 10) $-\sqrt{54} - 3\sqrt{6} + 3\sqrt{27}$
- 11) $-3\sqrt{6} - \sqrt{12} + 3\sqrt{3}$
- 12) $-\sqrt{5} - \sqrt{5} - 2\sqrt{54}$
- 13) $3\sqrt{2} + 2\sqrt{8} - 3\sqrt{18}$
- 14) $2\sqrt{20} + 2\sqrt{20} - \sqrt{3}$
- 15) $3\sqrt{18} - \sqrt{2} - 3\sqrt{2}$
- 16) $-3\sqrt{27} + 2\sqrt{3} - \sqrt{12}$
- 17) $-3\sqrt{6} - 3\sqrt{6} - \sqrt{3} + 3\sqrt{6}$
- 18) $-2\sqrt{2} - \sqrt{2} + 3\sqrt{8} + 3\sqrt{6}$
- 19) $-2\sqrt{18} - 3\sqrt{8} - \sqrt{20} + 2\sqrt{20}$
- 20) $-3\sqrt{18} - \sqrt{8} + 2\sqrt{8} + 2\sqrt{8}$
- 21) $-2\sqrt{24} - 2\sqrt{6} + 2\sqrt{6} + 2\sqrt{20}$
- 22) $-3\sqrt{8} - \sqrt{5} - 3\sqrt{6} + 2\sqrt{18}$
- 23) $3\sqrt{24} - 3\sqrt{27} + 2\sqrt{6} + 2\sqrt{8}$
- 24) $2\sqrt{6} - \sqrt{54} - 3\sqrt{27} - \sqrt{3}$
- 25) $-2\sqrt[3]{16} + 2\sqrt[3]{16} - 2\sqrt[3]{2}$
- 26) $3\sqrt[3]{135} - \sqrt[3]{81} - \sqrt[3]{135}$
- 27) $2\sqrt[4]{243} - 2\sqrt[4]{243} - \sqrt[4]{3}$
- 28) $-3\sqrt[4]{4} + 3\sqrt[4]{324} + 2\sqrt[4]{64}$
- 29) $3\sqrt[4]{2} - 2\sqrt[4]{2} - \sqrt[4]{243}$
- 30) $2\sqrt[4]{6} + 2\sqrt[4]{4} + 3\sqrt[4]{6}$
- 31) $-\sqrt[4]{324} + 3\sqrt[4]{324} - 3\sqrt[4]{4}$
- 32) $-2\sqrt[4]{243} - \sqrt[4]{96} + 2\sqrt[4]{96}$
- 33) $2\sqrt[4]{2} + 2\sqrt[4]{3} + 3\sqrt[4]{64} - \sqrt[4]{3}$
- 34) $2\sqrt[4]{48} - 3\sqrt[4]{405} - 3\sqrt[4]{48} - \sqrt[4]{162}$
- 35) $-3\sqrt[5]{6} - \sqrt[5]{64} + 2\sqrt[5]{192} - 2\sqrt[5]{160}$
- 36) $2\sqrt[5]{256} - 2\sqrt[7]{256} - 3\sqrt[7]{2} - \sqrt[7]{640}$
- 37) $2\sqrt[5]{160} - 2\sqrt[5]{192} - \sqrt[5]{160} - \sqrt[5]{-160}$
- 38) $-2\sqrt[7]{256} - 2\sqrt[7]{256} - 3\sqrt[7]{2} - \sqrt[7]{640}$
- 39) $-\sqrt[6]{256} - 2\sqrt[6]{4} - 3\sqrt[6]{320} - 2\sqrt[6]{128}$
- 40) $-3\sqrt[7]{3} - 3\sqrt[7]{768} + 2\sqrt[7]{384} + 3\sqrt[7]{5}$



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8.3

Answers - Add and Subtract Radicals

1) $6\sqrt{5}$

21) $-4\sqrt{6} + 4\sqrt{5}$

2) $-3\sqrt{6} - 5\sqrt{3}$

22) $-\sqrt{5} - 3\sqrt{6}$

3) $-3\sqrt{2} + 6\sqrt{5}$

23) $8\sqrt{6} - 9\sqrt{3} + 4\sqrt{2}$

4) $-5\sqrt{6} - \sqrt{3}$

24) $-\sqrt{6} - 10\sqrt{3}$

5) $-5\sqrt{6}$

25) $2\sqrt[3]{2}$

6) $-3\sqrt{3}$

26) $6\sqrt[3]{5} - 3\sqrt[3]{3}$

7) $3\sqrt{6} + 5\sqrt{5}$

27) $-\sqrt[4]{3}$

8) $-\sqrt{5} + \sqrt{3}$

28) $10\sqrt[4]{4}$

9) $-8\sqrt{2}$

29) $\sqrt[4]{2} - 3\sqrt[4]{3}$

10) $-6\sqrt{6} + 9\sqrt{3}$

30) $5\sqrt[4]{6} + 2\sqrt[4]{4}$

11) $-3\sqrt{6} + \sqrt{3}$

31) $3\sqrt[4]{4}$

12) $-2\sqrt{5} - 6\sqrt{6}$

32) $-6\sqrt[4]{3} + 2\sqrt[4]{6}$

13) $-2\sqrt{2}$

33) $2\sqrt[4]{2} + \sqrt[4]{3} + 6\sqrt[4]{4}$

14) $8\sqrt{5} - \sqrt{3}$

34) $-2\sqrt[4]{3} - 9\sqrt[4]{5} - 3\sqrt[4]{2}$

15) $5\sqrt{2}$

35) $\sqrt[5]{6} - 6\sqrt[5]{2}$

16) $-9\sqrt{3}$

36) $10\sqrt[5]{6} - 9\sqrt[5]{5}$

17) $-3\sqrt{6} - \sqrt{3}$

37) $4\sqrt[5]{5} - 4\sqrt[5]{6}$

18) $3\sqrt{2} + 3\sqrt{6}$

38) $-11\sqrt[7]{2} - 2\sqrt[7]{5}$

19) $-12\sqrt{2} + 2\sqrt{5}$

39) $-4\sqrt[6]{4} - 6\sqrt[6]{5} - 4\sqrt[6]{2}$

20) $-3\sqrt{2}$

40) $\sqrt[7]{3} - 6\sqrt[7]{6} + 3\sqrt[7]{5}$



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